Single-zone zero-dimensional model study for diesel-fuelled homogeneous charge compression ignition (HCCI) engines using Cantera

A. Aziz Hairuddin¹*, Talal Yusaf² and Andrew P. Wandel³

¹Department of Mechanical and Manufacturing Engineering
Faculty of Engineering, Universiti Putra Malaysia,
43400 UPM Serdang, Selangor, Malaysia.
*Email: ahziz@upm.edu.my
²National Centre for Engineering in Agriculture,
School of Mechanical and Electrical Engineering
University of Southern Queensland, Toowoomba, 4350 QLD, Australia
³Computational Engineering and Science Research Centre
School of Mechanical and Electrical Engineering
University of Southern Queensland, Toowoomba, 4350 QLD, Australia.

ABSTRACT

Homogeneous charge compression ignition (HCCI) engine technology is relatively new and the combustion behavior in an HCCI engine is difficult to predict. The combustion is fully controlled by the chemical kinetics and the chemical reaction of the mixture is influenced by changing input parameters. A zero-dimensional single-zone model was used to investigate the combustion behavior of a diesel engine operating in HCCI mode. An open source chemical kinetics package from Cantera was used in this study. The combustion behaviour can be observed, where H₂O₂ was fully decomposed during the main combustion event. The time for H₂O₂ to completely decompose into OH radicals was very short, which was about 5°CA. The combustion phasing was predicted in accordance with the experiment. The auto-ignition can be controlled by controlling the intake temperature or AFR. The start of combustion was advanced by increasing the intake temperature from 20 to 70°C and reducing the AFR from 58 to 29. However, reducing AFR will increase the in-cylinder peak pressure. In general, a zero-dimensional model is a useful and faster tool to predict the combustion phasing. When coupled with chemical kinetics, it provides more accurate results.

Keywords: diesel, HCCI, Cantera, n-heptane, single-zone, zero-dimensional.

INTRODUCTION

Homogeneous charge compression ignition (HCCI) engines have received increasing attention recently because of their advantages in reducing emissions levels, such as NOₓ [1-6]. An attempt by regulatory bodies, such as those in Europe, the United States (US) and Japan, to reduce emissions levels from conventional engines [7-9] has made the HCCI engines a viable alternative for low emissions engines. Electric vehicles offer virtually zero emissions; however, battery technology used in electric vehicles has not matured sufficiently. Primary disadvantages include a longer recharge time and limited mileage per charge. If global emissions (from vehicles, industries and electric power generators, among others) are to be the major concerns, electric vehicles still have emissions generated from the power plant generator. The power plant generator usually uses
conventional engines to get electric energy, except when using renewable energy sources (such as hydropower, solar or wind turbine). Thus, this is where the HCCI engine comes into place, where it can be used in any engine configuration: stationary, vehicles or ship engines.

An HCCI engine can be considered a new technology, even though the first research associated with it (with gasoline fuel) dated back to 1979, by Onishi et al. [10]. The HCCI technique is the process by which a homogeneous mixture of air and fuel is compressed until auto-ignition occurs near the end of the compression stroke, followed by a combustion process that is significantly faster than either compression ignition (CI) or spark ignition (SI) combustion [11-14]. The air/fuel mixture quality in HCCI engines is generally lean, auto-ignites in multiple locations and is then burned volumetrically without discernible flame propagation [15-18]. Combustion occurs when the homogeneous mixture has reached its chemical activation energy and is fully controlled by chemical kinetics [19], rather than by a spark or injection timing. Because the chemical kinetics fully control the mixture, the engine is difficult to start in cold conditions. Apart from that, the disadvantages of HCCI engines are as follows: 1) difficult to control the auto-ignition; 2) they have a high heat release rate at high loads; 3) they have high levels of unburned hydrocarbon (UHC) and carbon monoxide and 4) they knock under certain operating conditions [20-23]. However, an HCCI engine offers some advantages, wherein the following occur: 1) there is a high engine efficiency relative to spark ignition (SI) engines [24, 25]; 2) there is the ability to operate on a wide range of fuels [25-27]; and 3) there is the ability to be used in any engine configuration [28-30].

A diesel-fuelled engine was investigated in this study because the engine is stronger due to it having higher torque than SI engines, as well as the fact that it is mostly used in agricultural areas [12, 31-34]. The engine could be used in a stationary form or for vehicles. The use of an HCCI configuration for a diesel-fuelled engine could be the future of diesel engines due to the advantages in producing ultra-low nitrogen oxides (NO\textsubscript{x}), soot emissions and higher fuel conversion efficiency [35-37]. Biodiesel could also be used in HCCI engines, as it currently receives increasing attention from researchers worldwide [38-44] as a renewable energy or for vehicle engines. Various researchers have investigated the HCCI engine both experimentally [45-48] and numerically [45, 49-51]. Many numerical studies used a computational fluid dynamics (CFD) approach to obtain more accurate results of combustion temperature and products [52-59]. A CFD approach uses more computational power and time compared to a single-zone thermodynamics simulation. Thermodynamics models are unable to match the CFD results in terms of accuracy; however, they are still able to predict a combustion behavior comparable to experiments [60].

Better agreement in combustion phasing is achieved when the thermodynamics model is coupled with detailed chemical kinetics and turbulent mixing effects [15]. The purpose of this paper was to study the combustion behavior of diesel-fuelled HCCI engines using the thermodynamics single-zone zero-dimensional model, coupled with Cantera [61] as a chemical kinetics library. Cantera is an open-source chemical kinetics library that has not been widely used in engine simulations. Most of the numerical studies in engines today used Chemkin as a chemical kinetics library [62-64], which is no longer freely available. The availability of an open-source library is, therefore, beneficial for new researchers. This study discusses the numerical model used in Section 2, followed by its validation in Section 3 along with the chemical reactions mechanism and methods of controlling the auto-ignition. The paper closes with the conclusion in Section 4.

METHODS AND MATERIALS
A zero-dimensional model uses time as the independent variable to model the combustion in the chamber. Time can be represented by $\theta$, which is the CA, because $\theta$ monotonically increases with time. In the next sub-sections, the equations used to model the zero-dimensional environment for a single-cylinder engine are discussed. The zero-dimensional model used in this study was initially developed by Assanis and Heywood [65]. However, some changes had been made: the current model used a different heat release rate model, a different valve motion model and utilised a detailed chemical reaction mechanism. The simulation began from the inlet valve open (IVO) and until the exhaust valve open (EVO) and the thermodynamics properties were assumed to be uniform throughout the combustion chamber. Then, all of the equations pertaining to the simulation were coded using the Matlab software, combined with an open-source chemical kinetics package.

**Engine Geometry**
The instantaneous volume at any crank angle position can be obtained from

$$V_i = V_c \left[ 1 + \frac{R_c - 1}{2} \left( R + 1 - \cos \theta - \sqrt{R^2 - \sin^2 \theta} \right) \right] \quad (1)$$

where, $V_c$ is the clearance volume, $R_c$ is the compression ratio, and $R$ is the connecting rod length. Differentiating equation (1) with respect to the crank angle, the rate of the change of volume is represented by

$$\frac{dV}{d\theta} = V_c \left[ \frac{R_c - 1}{2} \left( \sin \theta \right) \left( \frac{1 + \cos \theta}{\sqrt{R^2 - \sin^2 \theta}} \right) \right] \quad (2)$$

The change in volume is an important parameter, as these equations will be used to determine the piston work.

**Conservation of Mass**
The model of the thermodynamics system is an open system; thus, the mass flows in and out of the system, governing the total mass of the chamber

$$\frac{dm}{dt} = \sum_j \dot{m}_j \quad (3)$$

where, $\dot{m}$ is the mass flow rate, $m$ is the mass and the $j$ is the number of flows in or out of the system.

**Conservation of Energy**
The energy equation was derived from the first law of thermodynamics for an open system

$$\frac{d\mu}{dt} = \frac{dQ}{dt} - P \frac{dV}{dt} + \sum_j \dot{m}_j h_j \quad (4)$$

where, $\mu$ is the specific internal energy, $Q$ is the net heat transfer, $P$ is the in-cylinder pressure, $V$ is the instantaneous cylinder volume and $h$ is the specific enthalpy. After
manipulating equation (4) (the derivation is shown in the appendices), the final equation for temperature changes in a zero-dimensional single-zone model is given [65] by

\[
\frac{dT}{dt} = \frac{1}{\bar{C}_p} \left[ \frac{P_v \sum_i R_i}{R_u} - \sum_i h_i \right] \frac{dY_i}{dt} - \frac{\bar{m}}{m} (h - P_v)
\]

\[
+ \frac{1}{m} \left( \frac{dQ_h}{dt} - P \frac{dV}{dt} + \sum_j \bar{m}_j h_j \right)
\]

(5)

In equation (5), \(\bar{C}_p\) is the specific heat at constant pressure, \(T\) is the instantaneous in-cylinder temperature, \(v\) is the specific volume, \(R_u\) is the universal heat constant, \(Y_i\) is the mass fraction of species \(i\), \(\bar{m}_i\) is the mass flow rate into the cylinder and \(Q_h\) is the heat loss to the cylinder wall. The derivation of equation (5) was discussed extensively by Assanis and Heywood [65]. Once the instantaneous in-cylinder temperature was obtained, the in-cylinder pressure will then be determined using the ideal gas equation, as

\[
P = \frac{\rho R_u T}{\bar{W}_{mw}} \quad \text{with} \quad \bar{W}_{mw} = \frac{1}{\sum^n_i Y_i / W_i}
\]

(6)

where, \(\bar{W}_{mw}\) is the mean molecular weight of the mixture, \(\rho\) is the density, \(W_i\) is the molecular weight of the \(i\)th species and \(n\) is the total number of species.

The volume in equation (5) as a function of crank angle (CA), \(\theta\), is given by

\[
V = V_c \left[ 1 + \frac{R_c - 1}{2} \left( R + 1 - \cos \theta - \sqrt{R^2 - \sin^2 \theta} \right) \right]
\]

(7)

where \(V_c\) is the clearance volume, \(R\) is the ratio of connecting rod length to crank radius and \(R_c\) is the compression ratio.

To obtain the mass flow rate in and out of the chamber, the valve motion had to be modelled. Thus, to model the valve lift across the entire CA, a model from Assanis and Polishak [66] was employed. The valve lift profile, \(y\), was determined by using the desired maximum valve lift \(L_v\) and half-event angle \(c\), then the profile as a function of CA is

\[
y = L_v + C_2 \theta^2 + C_w \theta^w + C_q \theta^q + C_r \theta^r + C_s \theta^s
\]

(8)

where \(w, q, r\) and \(s\) are constants to match the desired valve lift curve, which are selected as \(w = 6, q = 8, r = 10\) and \(s = 12\). The coefficients are

\[
C_2 = \frac{-wqrsL_v}{[(w-2)(q-2)(r-2)(s-2)c^2]}
\]

(9)

\[
C_w = \frac{2wqrsL_v}{[(w-2)(q-w)(r-w)(s-w)c^w]}
\]

(10)

\[
C_q = \frac{-2wqrsL_v}{[(q-2)(q-w)(r-q)(s-q)c^q]}
\]

(11)
Single-zone zero-dimensional model study for diesel-fuelled homogeneous charge compression ignition (HCCI) engines using Cantera

\[
C_r = \frac{2wqsL_v}{(r-2)(r-w)(r-q)(s-r)c^r}
\]

(12)

\[
C_s = \frac{-2wqrL_v}{(s-2)(s-w)(s-q)(s-r)c^s}
\]

(13)

By using equation (8), a typical valve lift profile with tappet mechanism (mechanical lifters) is illustrated in Figure 1. Once the valve lift is known, the effective valve open area can be obtained. In this case, the effective valve open area was taken to be its curtain area, which is given by

\[
A_c = \pi D_v L_v
\]

(14)

In general, larger valve sizes (or more valves per cylinder) give higher maximum air flows in and out of the chamber. The mass flow rate to the combustion chamber can then be obtained by using the equation of compressible flow through a flow restriction [67]. The equation includes real gas flow effects with discharge coefficient \(C_d\) obtained from experiments [68]. In principle, the mass flows in or out of the combustion chamber, when there is a pressure difference between the chamber and ports. The equation is separated into two cases: choked and subsonic flows. For choked flow,

\[
\left( \frac{p_T}{p_0} \leq \left[ \frac{2}{\gamma + 1} \right]^{\gamma/\gamma-1} \right)
\]

\[
m_{in} = \frac{C_d A_c p_0}{\sqrt{RT_0}} \sqrt{\gamma} \left[ \frac{2}{\gamma + 1} \right]^{\gamma+1/2(\gamma-1)}
\]

(15)

while for subsonic flow,

\[
\left( \frac{p_T}{p_0} > \left[ \frac{2}{\gamma + 1} \right]^{\gamma/\gamma-1} \right)
\]

\[
m_{in} = \frac{C_d A_c p_0}{\sqrt{RT_0}} \left( \frac{p_T}{p_0} \right)^{1/\gamma} \left\{ \frac{2\gamma}{\gamma - 1} \left[ 1 - \left( \frac{p_T}{p_0} \right)^{\gamma-1/\gamma} \right] \right\}^{1/2}
\]

(16)

where \(p_T, p_0, T_0\) and \(\gamma\) are the downstream static pressure, upstream stagnation pressure, upstream stagnation temperature and ratio of specific heats, respectively. Equations (15) and (16) are functions of gas properties, valve geometry and thermodynamic states upstream and downstream of the valves. For flow into the combustion chamber, \(p_0\) is the intake port pressure and \(p_T\) is the cylinder pressure. On the other hand, \(p_0\) is the cylinder pressure and \(p_T\) is the exhaust port pressure for the flow out of the combustion chamber. The value \(C_d\) was obtained experimentally from Stiesch [68]. Once the mass flow rate was determined, it will be used in the energy equation and also to obtain the total mass in the combustion chamber.
Conservation of Species
The chemical reactions are the source term in the energy equation, wherein the
temperature changes based on the energy being transferred from one form to another due
to chemical reactions. Modeling the combustion with a chemical reaction mechanism is
critical because chemical kinetics fully control the HCCI engines. In this study, an n-
heptane reduced mechanism [69] was used as a surrogate fuel to simulate diesel
combustion. This was chosen because n-heptane’s chemical properties are similar to that
of conventional diesel in terms of the cetane number. The mechanism consists of 160
species and 770 elementary reactions. Thus, the change of mass fraction of each species
due to chemical reactions is given by

\[ \frac{dY_i}{dt} = \frac{\dot{\omega}_i W_{mw}}{\rho}, \quad i = 1, \ldots, n \]  

(17)

where, \( \dot{\omega}_i \) is the molar production rate. The Cantera package was used to solve the
chemical reaction mechanism. A readily available n-heptane mechanism file in the
Chemkin format was then converted to Cantera format so that it could be used with the
Cantera package. There was no change in the chemical reaction mechanisms; thus, no
validation was required as of the chemical kinetics itself.

Heat Transfer
Heat is transferred between the cylinder walls and cylinder gases via convection and
radiation. The radiation effect is neglected in HCCI engines because the convective force
from the gases to the cylinder walls is dominant in the heat transfer mechanism [70]. In
the thermodynamics model, the convective heat transfer was predicted to match the
experimental results because the model did not permit a full prediction of the in-cylinder
gas motion [71]. The convective heat transfer rate can be described by Newton’s law of
cooling [72], as given by
\[ \frac{dQ_n}{dt} = h_c A_w (T - T_w) \]  

(18)

where, \( h_c \) is the heat transfer coefficient, \( A_w \) is the cylinder wall area and \( T_w \) is the wall temperature. The wall area is the sum of the cylinder wall, piston crown, and cylinder head areas. In a zero-dimensional simulation, the heat transfer coefficient has to be modeled, wherein the model attempts to reproduce the heat release rate obtained from the experiments. In this study, a modified Woschni heat transfer coefficient model was used, in which the model had been developed for HCCI engines; the measurements were taken in the piston crown and cylinder head areas [72]. The equation is given by

\[ h_c = 194.7 L^{-0.2} P^{0.8} T^{-0.73} (v_{tuned})^{0.8} \]  

(19)

where, the characteristic velocity \( v_{tuned} \) is

\[ v_{tuned} = C_1 \bar{s}_p + C_2 \frac{V_d T_r}{6 P_r V_r} (P - P_{mot}) \]  

(20)

In equation (19) and (20), \( L \) is the characteristic length scale, \( C_1 \) and \( C_2 \) are constants with values 2.28 and 0.00324, respectively, \( V_d \) is the displacement volume, subscript \( r \) is the reference condition, and \( P_{mot} \) is the motoring pressure: a cylinder pressure without combustion. The effect of different heat transfer coefficient models had been discussed by Hairuddin, Wandel [1].

Table 1. Engine parameters used in the current study, ATDC is after top dead center, ABDC is after bottom dead center, BBDC is before bottom dead center [73].

<table>
<thead>
<tr>
<th>Engine Parameters</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Cylinder bore</td>
<td>82.55 mm</td>
</tr>
<tr>
<td>Stroke</td>
<td>114.3 mm</td>
</tr>
<tr>
<td>Connecting rod length</td>
<td>254 mm</td>
</tr>
<tr>
<td>Compression ratio (CR)</td>
<td>10</td>
</tr>
<tr>
<td>Engine speed</td>
<td>900 rpm</td>
</tr>
<tr>
<td>Inlet valve open (IVO)</td>
<td>10° CA ATDC</td>
</tr>
<tr>
<td>Inlet valve closed (IVC)</td>
<td>36° CA ABDC</td>
</tr>
<tr>
<td>Exhaust valve open (EVO)</td>
<td>40° CA BBDC</td>
</tr>
<tr>
<td>Exhaust valve closed</td>
<td>5° CA ATDC</td>
</tr>
</tbody>
</table>

RESULTS AND DISCUSSION

The model was validated against experimental results before proceeding with further analysis, where the experiment was run by using n-heptane as a fuel with port injection in a single-cylinder HCCI engine [73]. The model was also compared with their thermodynamics model. The engine parameters used in this study are shown in Table 1. The mixing effect must be taken into consideration because the fuel was port injected; thus, the effective intake temperature was set 20°C higher than the desired intake temperature [73]. Therefore, the intake temperature for the zero-dimensional model in this study was increased to 333 K for the intake temperature of 313 K. The simulation result was compared with the experimental data and another single-zone model in Figure
2. The validated result was completed using a modified Woschni heat transfer coefficient with an air-to-fuel ratio (AFR) of 50. The in-cylinder peak pressure was slightly higher than the experiment due to the limitation of the zero-dimensional single-zone model: it was assumed that the entire combustion chamber was homogeneous. Overall, the combustion phasing was in good agreement with the experimental data, demonstrating that the single-zone model was suitable for use in diesel HCCI engine simulations.

![Figure 2. Comparison between single-zone zero-dimensional model with the experiment and another single-zone model using modified Woschni heat transfer coefficient model [73]. CR=10.0, N=900 rpm, T_{in}=40°C, P_{in}=95 kPa, AFR=50](image)

**Chemical Reactions**

The combustion event can be observed when there is a sharp increase in the temperature, as shown in Figure 3. This occurred when the piston approached the top dead center. Then, the ignition occurred when the temperature reached between 1000 and 1100 K. The combustion in HCCI engines was fully controlled by chemical kinetics and Flowers, Aceves [74] have described the HCCI ignition by H\(_2\)O\(_2\) decomposition. Figure 3 shows that radicals H\(_2\)O\(_2\), HO\(_2\) and OH were selected because these were the most important in driving the ignition process. H\(_2\)O\(_2\) and HO\(_2\) were related with LTR, wherein these radicals started to accumulate when the temperature was between 800 and 900K. OH had reached its first peak when LTR occurred and it started to accumulate again when approaching the HTR region. Once the in-cylinder temperature reached 1000–1100 K, H\(_2\)O\(_2\) decomposed rapidly and formed a significant amount of OH radicals [60]. The fuel (nC\(_7\)H\(_{16}\)) was consumed when OH was formed; at the same time, the amount of H\(_2\)O\(_2\) reduced rapidly. The amount of fuel started to decrease at the LTR region by forming H\(_2\)O\(_2\) and HO\(_2\). The fuel was completely being consumed when OH radicals reached their peak during the main combustion event: H\(_2\)O\(_2\) had been fully decomposed. The time for H\(_2\)O\(_2\) to completely decompose into OH radicals was very short, which was about 5°CA. If the engine speed was increased, the chance for H\(_2\)O\(_2\) to form enough amount of OH to
consume the fuel was very minimal. This would create a combustion that was difficult to achieve when the engine speed was increased and HCCI was not achievable in this condition. In general, the combustion event for a diesel HCCI engine can be seen in this model using the Cantera package and could be used in future studies.

Figure 3. Species mass fraction of nC\textsubscript{7}H\textsubscript{16}, H\textsubscript{2}O\textsubscript{2}, HO\textsubscript{2} and OH along with the temperature trend during combustion events. The figure is enlarged within the red circle to increase the image of the mass fraction trend of HO\textsubscript{2} and OH. Simulated at CR=10.0, N=900 rpm, T\textsubscript{in}=40°C, P\textsubscript{in}=95 kPa, AFR=50.
Figure 4. The difference in in-cylinder pressure when simulated at different engine speeds with the same operating condition: CR=10.0, T_{in}=40°C, P_{in}=95 kPa, AFR=50.

**Effect of Varying Engine Speed**

The engine speed is one of the factors that influence the chemical reactions: higher engine speeds require fast combustion. When the engine was operated at the same condition, increasing the engine speed from 900 to 1500 rpm will stop the HCCI combustion, as shown in Figure 4. The maximum in-cylinder temperature at 1500 rpm was about 700 K, which was not enough to initiate the accumulation of H$_2$O$_2$ and HO$_2$. Figure 5 shows the mass fraction comparison of H$_2$O$_2$, nC$_7$H$_{16}$ and OH between the two different engine speeds: 900 and 1500 rpm. At 900 rpm, the fuel was entirely consumed when the OH was fully formed due to the decomposition of H$_2$O$_2$. The amount of fuel also started to reduce when the radical H$_2$O$_2$ began to accumulate. However, at a higher engine speed (1500 rpm), there was no accumulation of H$_2$O$_2$. This was because there was not enough time for H$_2$O$_2$ and HO$_2$ to start the reactions. The radical HO$_2$ was not shown in the figure because the amount was very small. Thus, there was no reduction in fuel mass fraction, which indicated there was no combustion at 1500 rpm, given the same operating condition. Therefore, increasing the engine speed without changing any of the factors resulted in a no combustion event occurring, in addition to the difficulty in controlling the ignition timing. Increasing the engine speed was necessary when more loads were required from the engine. The fuel will become more susceptible to combustion by increasing its chemical energy. This was achieved by changing a few other parameters, such as the intake temperature or AFR to the mixture; these parameters can be used to control the ignition timing of a diesel HCCI engine.

**Effect of Intake Temperature**

Intake air temperature is an important factor for controlling the auto-ignition timing of HCCI engines. Different fuels have different auto-ignition points and some of them require pre-heating to achieve good combustion. If methane or natural gas is used as a fuel, the intake air temperature has to be set to at least 400 K to achieve an appropriate ignition [75]. Therefore, the intake temperature will affect the auto-ignition point for other
fuels as well and increasing the intake temperature will reduce the ignition delay. Thus, the auto-ignition timing can be controlled.

Figure 5. Species mass fraction comparison of H$_2$O$_2$, nC$_7$H$_{16}$ and OH at two different engine speeds: 900 and 1500 rpm. Simulated at CR=10.0, T$_{in}$=40°C, P$_{in}$=95 kPa, AFR=50.

Figure 6. Effect of intake temperature on the in-cylinder pressure: CR=10.0, N=900 rpm, P$_{in}$=95 kPa, AFR=50 (a) Validated varying intake temperature against experimental from Guo et al. [59]; (b) Predicted in-cylinder pressure trend.
Figure 6 shows that the auto-ignition timing can be advanced once the intake temperature is increased. Results from the current simulation were compared with the experimental results [59] in Figure 6(a) to validate the model over different operating temperatures; the results were similar to those in Figure 2. An increase in air intake temperature will not affect the in-cylinder peak pressure significantly. Note the trend as the intake temperature increases: the predicted in-cylinder peak pressure starts to decrease, even though the auto-ignition is advanced, as shown in Figure 6(b). This trend was also observed in the experiment [73]. This is a good option for control because of the low increase in in-cylinder peak pressure.

Effect of AFR

The AFR is a measure of how much air and fuel is being consumed in the combustion chamber; diesel HCCI engines operated with lean mixtures (AFR > AFR_{stoich}) with AFR_{stoich} of about 14.5. Figure 7(a) shows the validated result of different AFRs compared with the experiment, again showing a good agreement. Meanwhile, Figure 7(b) shows the predicted result of reducing the AFR: an increase in the in-cylinder peak pressure and advancement of the auto-ignition timing. The in-cylinder peak pressure trend kept increasing with the reducing AFR, which will create knocking. In addition, the start of LTR was retarded with a reduction of AFR. However, if the mixture became too rich, the auto-ignition was advanced significantly, which will lead to knocking: an undesired combustion phenomenon. Therefore, careful tuning was needed to adapt to dynamic engine loads.

Figure 7. Effect of AFR on the in-cylinder pressure: CR=10.0, N=900 rpm, T_{in}=40°C, P_{in}=95 kPa (a) Validated varying AFR against the experiment from Guo et al. [59]; (b) Predicted in-cylinder pressure.
CONCLUSIONS

This paper had discussed a zero-dimensional model for a diesel HCCI engine using an open source chemical kinetics package, Cantera. The model had been validated and it was in agreement with the experimental data. In general, the following applied:

1. A zero-dimensional model is a useful and faster tool to predict the combustion phasing. A combination with chemical kinetics model gives relatively accurate results, provided that the conditions have been set correctly.
2. An open source chemical kinetics package, Cantera, is beneficial for researchers to simulate chemical reactions at no cost.
3. Three different heat transfer coefficient models had been investigated: the Woschni, modified Woschni, and Hohenberg models. The models are very sensitive to the temperature exponent under normal operating conditions. It was found that a modified Woschni correlation produced a more accurate result compared with the other two models and can be used for further analysis of a diesel HCCI engine.
4. Higher engine speed leads to a shorter decomposition time of H$_2$O$_2$ radicals. Thus, increasing the engine speed will make the HCCI combustion difficult to achieve when given the same operating conditions.
5. Intake temperature and AFR can be used as an ignition control for HCCI combustion. It was found that the combustion phasing was advanced by increasing all of the parameters (intake temperature, equivalence ratio, and energy ratio); therefore, the auto-ignition can be controlled.

ACKNOWLEDGEMENTS

The authors would like to be obliged to Universiti Putra Malaysia for providing research facilities and University of Southern Queensland for the research support. The study is also supported financially by IPM Putra Grant under project no. GP-IPM 9483100.

REFERENCES

Single-zone zero-dimensional model study for diesel-fuelled homogeneous charge compression ignition (HCCI) engines using Cantera


APPENDICES

The derivation of temperature changes in a zero-dimensional single-zone model from the first law of thermodynamics equations. The first law of thermodynamics equation is

\[ U = -W + Q_h + \sum_j m_j h_j \]  

where \( j \) is the number of flows entering or leaving the system. Differentiating equation (1) with time gives

\[ \frac{d(mu)}{dt} = -P \frac{dV}{dt} + \frac{dQ_h}{dt} + \sum_j \dot{m}_j h_j \]  

Knowing that the enthalpy for a homogenous system is defined as

\[ h = u + PV \]  

Substituting equation (3) to (2) yields

\[ \frac{d(mh)}{dt} - \frac{d(PV)}{dt} = \frac{dQ_h}{dt} - P \frac{dV}{dt} + \sum_j h_j \frac{dm_j}{dt} \]  

Manipulating of equation (4) becomes

\[ m \frac{dh}{dt} + h \frac{dm}{dt} - P \frac{dV}{dt} = \frac{dQ_h}{dt} - P \frac{dV}{dt} + \sum_j h_j \frac{dm_j}{dt} \]  

\[ m \frac{dh}{dt} = \frac{dQ_h}{dt} + V \frac{dP}{dt} - h \frac{dm}{dt} + \sum_j h_j \frac{dm_j}{dt} \]  

In equation (6), an expression of \( \frac{dh}{dt} \) in terms of changes in temperature needs to be developed. For a multi-component mixture of ideal gas and single phase,

\[ h = \sum_i Y_i h_i \quad \text{and} \quad h = h(T, P, Y_i) \]  

where, \( i \) is the component species in the mixture. Partial differentials with respect to temperature, pressure and composition are
Single-zone zero-dimensional model study for diesel-fuelled homogeneous charge compression ignition (HCCI) engines using Cantera

\[
\frac{dh}{dt} = \frac{\partial h}{\partial T} \bigg|_{P,Y_i} \frac{dT}{dt} + \frac{\partial h}{\partial P} \bigg|_{T,Y_i} \frac{dP}{dt} + \sum_i \frac{\partial h}{\partial Y_i} \bigg|_{P,T,Y_{i\neq j}} \frac{dY_i}{dt} \tag{8}
\]

The partial change of enthalpy with respect to pressure at constant temperature and composition is zero, hence equation (8) becomes

\[
\frac{dh}{dt} = C_p \frac{dT}{dt} + \sum_i h_i \frac{dY_i}{dt} \tag{9}
\]

The pressure gradient in equation (6) can be obtained by manipulating the equation of state for an ideal gas

\[
P V = mRT
\]

\[
P \frac{dV}{dt} + V \frac{dP}{dt} = mR \frac{dT}{dt} + T \frac{d(mR)}{dt}
\]

\[
P \frac{dV}{dt} + V \frac{dP}{dt} = mR \frac{dT}{dt} + T \frac{dR}{dt} + RT \frac{dm}{dt}
\]

\[
mT \frac{dR}{dt} = P \frac{dV}{dt} + V \frac{dP}{dt} - m \frac{dR}{dt} - RT \frac{dm}{dt} \tag{10}
\]

Dividing both sides of equation (10) with \(PV\) gives

\[
\frac{PV \frac{dR}{dt}}{R \frac{dt}} = \frac{mRT \frac{dV}{dt}}{V \frac{dt}} + \frac{mRT \frac{dP}{dt}}{P \frac{dt}} - \frac{PV \frac{dT}{dt}}{T \frac{dt}} - \frac{PV \frac{dm}{dt}}{m \frac{dt}} \tag{11}
\]

Rearranging equation (11) gives

\[
\frac{\dot{R}}{R} = \frac{mRT \frac{dV}{dt}}{PV \frac{dt}} + \frac{mRT \frac{dP}{dt}}{P \frac{dt}} - \frac{PV \frac{dT}{dt}}{T \frac{dt}} - \frac{PV \frac{dm}{dt}}{m \frac{dt}}
\]

Knowing that

\[
\dot{R} = \sum_i R_i \dot{Y}_i \tag{13}
\]

Substituting equation (13) to (12), and rearranging gives

\[
\dot{P} = P \left[ \frac{\sum_i R_i \dot{Y}_i}{R} + \frac{\dot{m}}{m} + \frac{\dot{T}}{T} - \frac{\dot{V}}{V} \right] \tag{14}
\]

Hence, substituting equation (14) to (6) and rearranging

\[
m \dot{h} = \sum_j m_j h_j + \dot{Q}_h + PV \left[ \frac{\sum_i R_i \dot{Y}_i}{R} + \frac{\dot{m}}{m} + \frac{\dot{T}}{T} - \frac{\dot{V}}{V} \right] - \dot{m} h
\]
\[
m \left( C_p \dot{T} + \sum_i h_i \dot{Y}_i \right) = \sum_j \dot{m}_j h_j + \dot{Q}_h + PV \left[ \frac{\sum_i R_i \dot{Y}_i}{R} + \frac{\dot{m}}{m} + \frac{\dot{T}}{T} - \dot{V} \right] - \dot{m} h
\]

\[
m C_p \dot{T} - PV \frac{\dot{T}}{T} = \sum_j \dot{m}_j h_j + \dot{Q}_h + \frac{PV}{R} \sum_i R_i \dot{Y}_i + \frac{PV}{m} \dot{m} - \dot{P} V - \dot{m} h
\]

\[
\dot{T} \left( m C_p - \frac{PV}{m T} \right) = \sum_j \dot{m}_j h_j + \dot{Q}_h + \frac{PV}{R} \sum_i R_i \dot{Y}_i + \frac{PV}{m} \dot{m} - \dot{P} V - \dot{m} h
\]

The final equation is

\[
\dot{T} = \frac{1}{A} \left[ \left( \frac{PV}{R} \sum_i R_i - \sum_i h_i \right) \dot{Y}_i - \frac{\dot{m}}{m} B + \frac{1}{m} \left( \frac{dQ_h}{dt} - P \frac{dV}{dt} + \sum_j \dot{m}_j h_j \right) \right] \quad (15)
\]

where,

\[
A = C_p - \frac{PV}{T} \quad \quad (16)
\]

\[
B = h - PV \quad \quad (17)
\]